



# WHAT WE WILL LEARN

**BINARY AND HEXADECIMAL NOTATIONS**

**ASCII AND UTF-8**

**LOGIC GATES AND BOOLEAN ALGEBRA**



# BINARY

In digital electronics and mathematics, binary is represented by a sequence of (*"1"s and "0"s*). It's a base-2 number system as opposed to decimal which is base-10.

Computers use binary numbers because designing electronic circuits is easier when dealing with simple switches represented by two states, i.e. binary states: (*"On" and "Off"*), (*"True" and "False"*).

Computers use binary to represent all data transported at the lowest levels. A 64 bit computer has a 64 bit data Bus that will transport 64 bits (binary digits) at once.

In the decimal system, there are 1s, 10s, 100s, ... positions (powers of 10 starting with 0)

In the binary system, there are 1s, 2s, 4s, 8s, ... positions (powers of 2 starting with 0)

Binary    Decimal equivalent

0    → 0

1    → 1

10   → 2

11   → 3

100 → 4



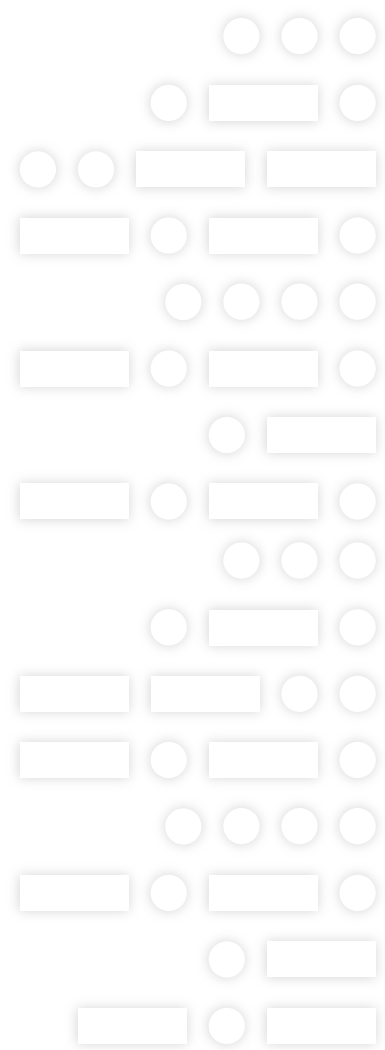
# BINARY: CONVERTING TO DECIMAL

Let's convert **110011** to decimal:

| (left-most bit) |           |          |          |          | (right-most bit) |
|-----------------|-----------|----------|----------|----------|------------------|
| <b>1</b>        | <b>1</b>  | <b>0</b> | <b>0</b> | <b>1</b> | <b>1</b>         |
| 32s digit       | 16s digit | 8s digit | 4s digit | 2s digit | 1s digit         |
| 1 x 32          | 1 x 16    | 0 x 8    | 0 x 4    | 1 x 2    | 1 x 1            |
| 32              | 16        | 0        | 0        | 2        | 1                |

Total: 51

Thus, 11011 in binary is equivalent to 51 in decimal.



# BINARY: ARITHMETIC - HOW TWO BINARY NUMBERS ARE ADDED.

How do we add binary numbers? (*similar to decimal numbers*)

1+1=2, so the extra 1 carries over to next digit.

$$\begin{array}{r} 11011 \\ + \quad 10 \\ \hline 11111 \end{array}$$

The diagram shows the binary addition of 11011 and 10. A carry of 1 is shown above the second digit from the right, with an arrow pointing to the first digit from the right. The result 11111 is shown below a horizontal line.



# BINARY: ARITHMETIC - NEGATIVE NUMBERS

We saw how positive numbers are represented in binary notation, but how to represent a negative binary number (-) ? A negative binary number is represented by an extra bit or sign bit. There are numerous methods that we can use, two of which are described below:

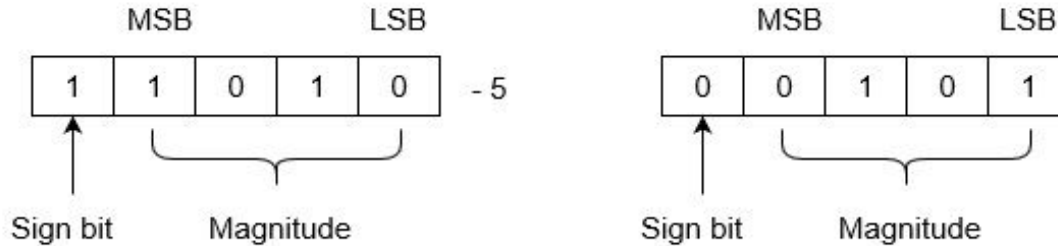
**1. Signed Magnitude Method** - using 5 bits register. The representation of -5 to +5 will be as follows:



In this method, number is divided into two parts: Sign bit and Magnitude. If the number is positive then sign bit will be 0 and if negative 1. Magnitude is represented with the binary form of the number to be represented.

# BINARY: ARITHMETIC - NEGATIVE NUMBERS

2. **1's Complement Method** - using 5 bits register. The representation of -5 and +5 will be as follows:



+5 is represented as it is represented in sign magnitude method. -5 is represented using the following steps:

(i)  $+5 = 0\ 0101$

(ii) Take 1's complement of  $0\ 0101$  and that is  $1\ 1010$ . MSB is 1 which indicates that number is negative.

MSB is always 1 in case of negative numbers.

# DATA: MEASURING

Bit - binary digit (0 or 1) - “Smallest unit of data”

Byte - 8 bits

Kilobyte (KB) - 1000 bytes - Kibibyte (KiB) - 1024 bytes

Megabit (Mb) -  $1000^2$  bits

Megabyte (MB) -  $10^6$  bytes - Mebibyte (MiB) -  $1024^3$  bytes

Gigabytes (GB) -  $10^9$  bytes - Gibibyte (GiB) -  $1024^6$  bytes

Terabytes (TB) -  $10^{12}$  bytes

Petabytes (PB) -  $10^{15}$  bytes





# DATA: TRANSFER RATES - SPEED OF SENDING DATA

Average number of bits or bytes transmitted (over a wire or wireless) in digital telecommunication.

Usually described by ISPs (Internet Service Providers) using either Megabits per second or Megabytes per second (Mbps or MB/s). It's important to make the distinction, otherwise you may well end up with a slower speed than anticipated.



# HEXADECIMAL NOTATION: INTRODUCTION

Binary in long sequences is difficult and cumbersome to read.

For software developers using 0s and 1s to represent our data would be extremely time consuming and tedious and prone to frequent errors and misrepresentations.

Developers use the Hexadecimal notation as a more compact form of encoding binary. Hexadecimal is a base 16 notation using numbers 0-9 and letters A-F.

However, computers cannot directly use hexadecimal notation to perform instructions. Hexadecimal notation is translated into binary before being processed. It is used as a convenience notation.



# HEXADECIMAL NOTATION

Below is a comparison between binary and hexadecimal notation:

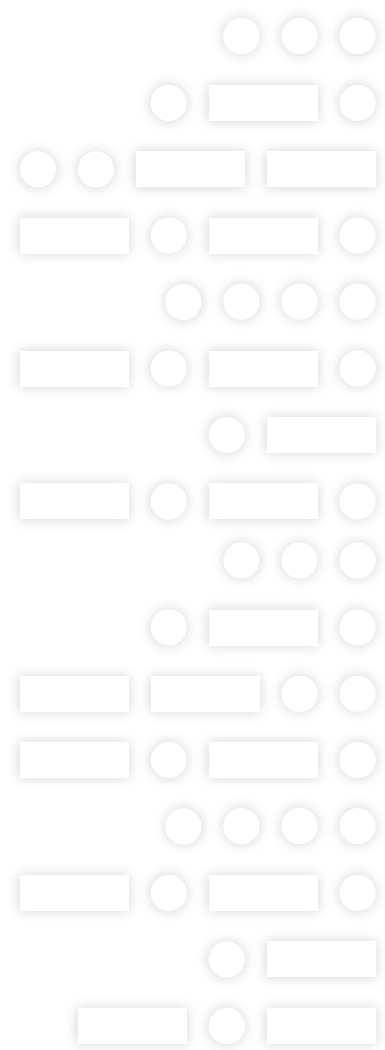
Binary (24 digits):

000111110000011110001010

Hexadecimal (6 digits):

1 F 0 7 8 A

Every 4 bits → 1 hexadecimal digit (1 - 9, and A - F)



# HEXADECIMAL NOTATION

| Decimal | Hex | Binary |
|---------|-----|--------|
| 0       | 0   | 0000   |
| 1       | 1   | 0001   |
| 2       | 2   | 0010   |
| 3       | 3   | 0011   |
| 4       | 4   | 0100   |
| 5       | 5   | 0101   |
| 6       | 6   | 0110   |
| 7       | 7   | 0111   |
| 8       | 8   | 1000   |
| 9       | 9   | 1001   |
| 10      | A   | 1010   |
| 11      | B   | 1011   |
| 12      | C   | 1100   |
| 13      | D   | 1101   |
| 14      | E   | 1110   |
| 15      | F   | 1111   |

Convert 1F048A to binary:

**1 F 0 4 8 A**

000111110000011110001010

# HEXADECIMAL NOTATION: COMMON USES

Amongst the uses of hexadecimal by Computer Scientist and software developers are:

1. Representing Colors - #000000 = 'black' and #ffffff = 'white'
2. Shorthand for Memory Locations - two hexadecimal digits for every byte as opposed to eight digits in binary.
3. Security hashes and secret keys
4. IPv6 Addresses
5. Represent Mac (Machine Access Codes)
6. Representing the Braille alphabet - Braille is a symbol language for the visually impaired.



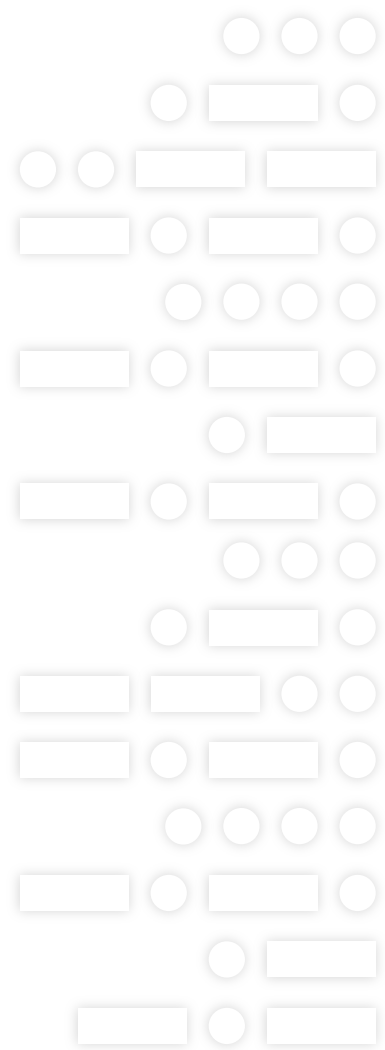
# ASCII NOTATION

We saw how numbers are represented in binary. How do we represent text, for example, text in our emails?

ASCII (American Standard Code for Information) is one solution: Ascii uses a byte (8-bits) for each character represented.

There are only 128 characters (since we have 8 digits,  $2^8 = 127$ ).

|    |     |     |     |     |    |    |    |     |    |     |    |     |     |    |
|----|-----|-----|-----|-----|----|----|----|-----|----|-----|----|-----|-----|----|
| H  | e   | l   | l   | o   | ,  | _  | R  | i   | c  | h   | a  | r   | d   | !  |
| 72 | 101 | 108 | 108 | 111 | 44 | 32 | 82 | 105 | 99 | 104 | 97 | 114 | 100 | 33 |



# ASCII NOTATION

The 128 Ascii characters can represent only the English alphabet.

| Dec | Hex | Oct | Char | Dec | Hex | Oct | Char    | Dec | Hex | Oct | Char | Dec | Hex | Oct | Char |
|-----|-----|-----|------|-----|-----|-----|---------|-----|-----|-----|------|-----|-----|-----|------|
| 0   | 0   | 0   |      | 32  | 20  | 40  | [space] | 64  | 40  | 100 | @    | 96  | 60  | 140 | `    |
| 1   | 1   | 1   |      | 33  | 21  | 41  | !       | 65  | 41  | 101 | A    | 97  | 61  | 141 | a    |
| 2   | 2   | 2   |      | 34  | 22  | 42  | "       | 66  | 42  | 102 | B    | 98  | 62  | 142 | b    |
| 3   | 3   | 3   |      | 35  | 23  | 43  | #       | 67  | 43  | 103 | C    | 99  | 63  | 143 | c    |
| 4   | 4   | 4   |      | 36  | 24  | 44  | \$      | 68  | 44  | 104 | D    | 100 | 64  | 144 | d    |
| 5   | 5   | 5   |      | 37  | 25  | 45  | %       | 69  | 45  | 105 | E    | 101 | 65  | 145 | e    |
| 6   | 6   | 6   |      | 38  | 26  | 46  | &       | 70  | 46  | 106 | F    | 102 | 66  | 146 | f    |
| 7   | 7   | 7   |      | 39  | 27  | 47  | '       | 71  | 47  | 107 | G    | 103 | 67  | 147 | g    |
| 8   | 8   | 10  |      | 40  | 28  | 50  | (       | 72  | 48  | 110 | H    | 104 | 68  | 150 | h    |
| 9   | 9   | 11  |      | 41  | 29  | 51  | )       | 73  | 49  | 111 | I    | 105 | 69  | 151 | i    |
| 10  | A   | 12  |      | 42  | 2A  | 52  | *       | 74  | 4A  | 112 | J    | 106 | 6A  | 152 | j    |
| 11  | B   | 13  |      | 43  | 2B  | 53  | +       | 75  | 4B  | 113 | K    | 107 | 6B  | 153 | k    |
| 12  | C   | 14  |      | 44  | 2C  | 54  | ,       | 76  | 4C  | 114 | L    | 108 | 6C  | 154 | l    |
| 13  | D   | 15  |      | 45  | 2D  | 55  | -       | 77  | 4D  | 115 | M    | 109 | 6D  | 155 | m    |
| 14  | E   | 16  |      | 46  | 2E  | 56  | .       | 78  | 4E  | 116 | N    | 110 | 6E  | 156 | n    |
| 15  | F   | 17  |      | 47  | 2F  | 57  | /       | 79  | 4F  | 117 | O    | 111 | 6F  | 157 | o    |
| 16  | 10  | 20  |      | 48  | 30  | 60  | 0       | 80  | 50  | 120 | P    | 112 | 70  | 160 | p    |
| 17  | 11  | 21  |      | 49  | 31  | 61  | 1       | 81  | 51  | 121 | Q    | 113 | 71  | 161 | q    |
| 18  | 12  | 22  |      | 50  | 32  | 62  | 2       | 82  | 52  | 122 | R    | 114 | 72  | 162 | r    |
| 19  | 13  | 23  |      | 51  | 33  | 63  | 3       | 83  | 53  | 123 | S    | 115 | 73  | 163 | s    |
| 20  | 14  | 24  |      | 52  | 34  | 64  | 4       | 84  | 54  | 124 | T    | 116 | 74  | 164 | t    |
| 21  | 15  | 25  |      | 53  | 35  | 65  | 5       | 85  | 55  | 125 | U    | 117 | 75  | 165 | u    |
| 22  | 16  | 26  |      | 54  | 36  | 66  | 6       | 86  | 56  | 126 | V    | 118 | 76  | 166 | v    |
| 23  | 17  | 27  |      | 55  | 37  | 67  | 7       | 87  | 57  | 127 | W    | 119 | 77  | 167 | w    |
| 24  | 18  | 30  |      | 56  | 38  | 70  | 8       | 88  | 58  | 130 | X    | 120 | 78  | 170 | x    |
| 25  | 19  | 31  |      | 57  | 39  | 71  | 9       | 89  | 59  | 131 | Y    | 121 | 79  | 171 | y    |
| 26  | 1A  | 32  |      | 58  | 3A  | 72  | :       | 90  | 5A  | 132 | Z    | 122 | 7A  | 172 | z    |
| 27  | 1B  | 33  |      | 59  | 3B  | 73  | ;       | 91  | 5B  | 133 | [    | 123 | 7B  | 173 | {    |
| 28  | 1C  | 34  |      | 60  | 3C  | 74  | <       | 92  | 5C  | 134 | \    | 124 | 7C  | 174 |      |
| 29  | 1D  | 35  |      | 61  | 3D  | 75  | =       | 93  | 5D  | 135 | ]    | 125 | 7D  | 175 | }    |
| 30  | 1E  | 36  |      | 62  | 3E  | 76  | >       | 94  | 5E  | 136 | ^    | 126 | 7E  | 176 | ~    |
| 31  | 1F  | 37  |      | 63  | 3F  | 77  | ?       | 95  | 5F  | 137 | _    | 127 | 7F  | 177 |      |

# UNICODE AND UTF-8

Ever wondered how computers manage to deal with all languages on websites, apps, keyboards, and output to printers etc. etc. Wonder no more, Unicode to the rescue.

ASCII can only support 128 characters for the English alphabet, computers needed a different solution for the many other languages out there, together using thousands of different characters, and then there are emojis! It's a complex alphabet soup!

Ü ç ๓ 😊

How do we represent them? We use Unicode and UTF-8


**Unicode:** Assigns a code for every character in the world.

**UTF-8:** Represents a unicode character in binary.





# UNICODE: DEFINES CODE POINTS FOR EVERY CHARACTER IN THE WORLD

| CHARACTER   | CODE POINT |
|---|------------|
| A   | U+0041     |
| a   | U+0061     |
| 0   | U+0030     |
| 9   | U+0039     |
| !   | U+0021     |
| Ü   | U+00DC     |
|   | ८ U+0683   |
| ८   | U+0C9A     |
|  | U+1F601    |

# UTF-8: DEFINES BINARY REPRESENTATION OF EVERY UNICODE CODEPOINT

| CHARACTER | CODE POINT | UTF-8 BINARY ENCODING                  |
|-----------|------------|--|
| A         | U+0041     | 01000001                               |
| a         | U+0061     | 01100001                               |
| o         | U+0030     | 00110000                               |
| 9         | U+0039     | 00111001                               |
| !         | U+0021     | 00100001                               |
| Ü         | U+00DC     | 11000011 10011100                      |
| ç         | U+0683     | 11011010 10000011                      |
| ☐         | U+2070E    | 11110000 10100000 10011100<br>10001110 |
| 😄         | U+1F601    | 11110000 10011111 10011000<br>10000001 |

# KEY ADVANTAGES OF UTF-8

- **Covers all languages:**  
Up-to 4 bytes allows the representation of millions of characters
- **Backward-compatible with ASCII:**  
Representation of “Hello, Richard!” is the same in ASCII and UTF-8
- **Spatial efficiency:**  
More frequent characters take less space

Unicode is probably one of the most useful concepts you can learn in software development, so go ahead and learn as much about it as you can.

Click the link for a great in-depth introduction to Unicode - [A great introduction to Unicode](#)



# SUMMARY: HOW HUMANS AND COMPUTERS REPRESENT NUMBERS AND TEXT

WHAT HUMANS CAN UNDERSTAND

48300 (Base-10)

WHAT COMPUTERS CAN UNDERSTAND

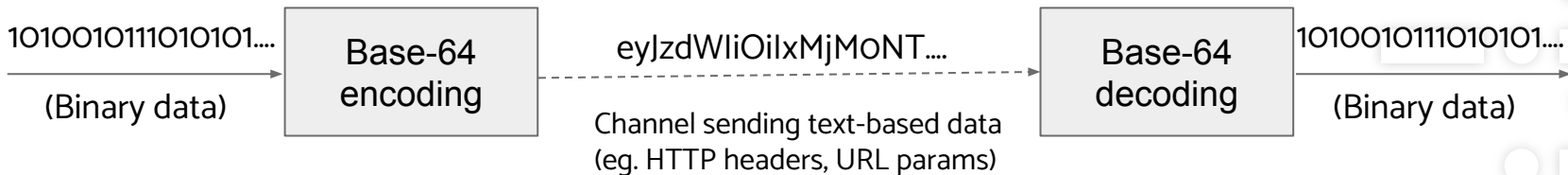
1011110010101100 (Binary)  
B C A C (Hex)

FETHİYE (Latin  
alphabet)

0100011001000101010101000100100011000100101100000101100101000101  
46455448c4b05945 UTF-8  
Hex

# BASE-64: ENCODING AND DECODING

Base-64 is a group of algorithms to represent raw binary data as textual data, for sending this data in a channel that only supports text-based data. All data is encoded into 64 characters.



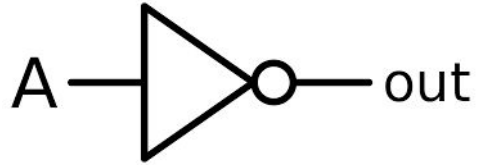
# LOGIC GATES AND BOOLEAN ALGEBRA

Logic gates are basically switches that derive a logical state/output depending on their inputs. The state is determined by a set of logical operations based on Boolean Algebra.

In computer science Truth Tables are used to represent logical expressions of True and False states using a set of Boolean Operators.

The most common Boolean operators are **AND**, **OR** and **NOT**. Each operator has a standard symbol that can be used when drawing logic gate circuits.

# NOT GATE



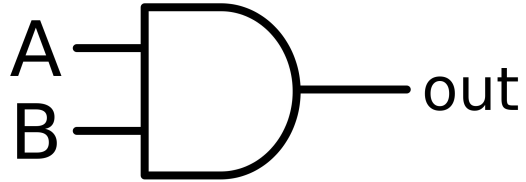
```
IF A is not true THEN  
  Do something...  
END
```

```
Example:  
IF speed is higher than 90 THEN  
  Reduce speed  
END
```

## Truth table

| A     | NOT A |
|-------|-------|
| false | true  |
| true  | false |

# AND GATE



IF A is true AND B is true THEN  
Do something...  
END

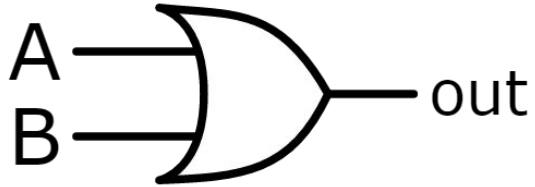
Example:  
IF it is raining AND it is cold THEN  
Take a coat  
END

**Truth table**

| A     | B     | A AND B |
|-------|-------|---------|
| false | false | false   |
| false | true  | false   |
| true  | false | false   |
| true  | true  | true    |



# OR GATE



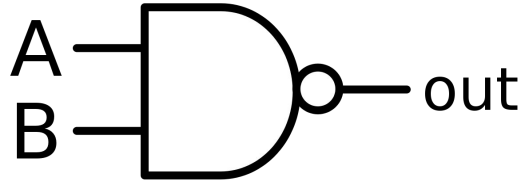
```
IF A is true OR B is true THEN  
  Do something...  
END
```

```
Example:  
IF it is raining OR it is too sunny THEN  
  Take an umbrella  
END
```

**Truth table**

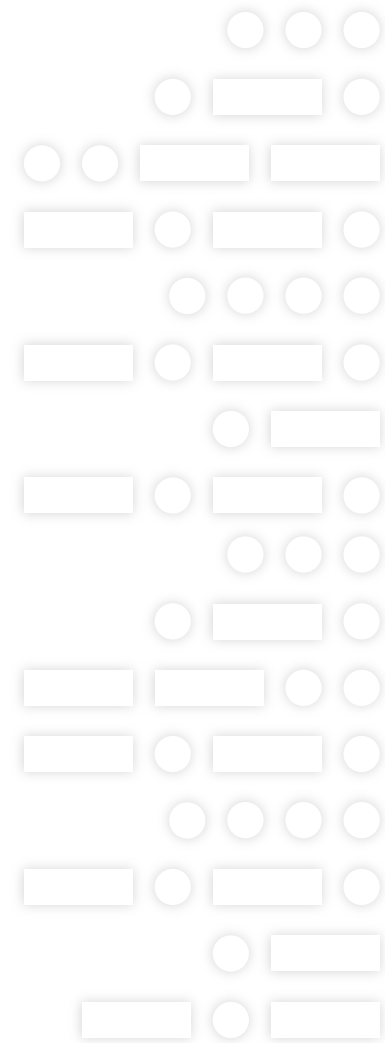
| A     | B     | A OR B |
|-------|-------|--------|
| false | false | false  |
| false | true  | true   |
| true  | false | true   |
| true  | true  | true   |

# NAND GATE

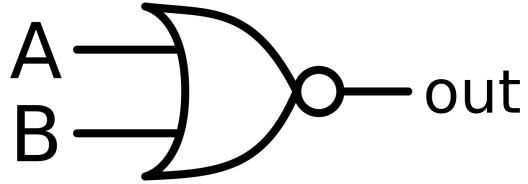


Truth table

| A         | B         | A AND B   |
|-----------|-----------|-----------|
| 0 / false | 0 / false | 1         |
| 0 / false | 1         | 1         |
| 1         | 0 / false | 1         |
| 1         | 1         | 0 / false |



# NOR GATE



**Truth table**

| A     | B     | A NOR B |
|-------|-------|---------|
| false | false | true    |
| false | true  | false   |
| true  | false | false   |
| true  | true  | false   |



# COMBINING OPERATIONS

| A | B | C | (NOT(A) AND B) OR NOT(C) |
|---|---|---|--------------------------|
| 0 | 0 | 0 | 1                        |
| 0 | 0 | 1 | 0                        |
| 0 | 1 | 0 | 1                        |
| 0 | 1 | 1 | 1                        |
| 1 | 0 | 0 | 1                        |
| 1 | 0 | 1 | 0                        |
| 1 | 1 | 0 | 1                        |
| 1 | 1 | 1 | 0                        |

